

## Inequalities:

### 1. Linear:

#### a. One variable:

##### i. Solving:

1. Solve normally by getting the variable by itself.
2. If you multiply or divide by a negative number, change the inequality sign

##### ii. Graphical Solution

1.  $>$  and  $<$  produce an open circle, test a point above and below the line to determine a TRUE value
2.  $\geq$  and  $\leq$  produce a closed circle, test a point above and below the line to determine a TRUE value

##### iii. Examples:

1.  $3x - 4 \leq 5$
2.  $-2x + 3 > 7$

#### b. Two variables:

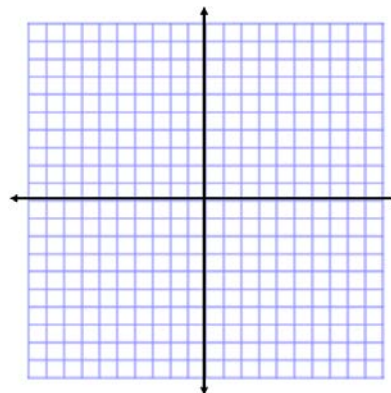
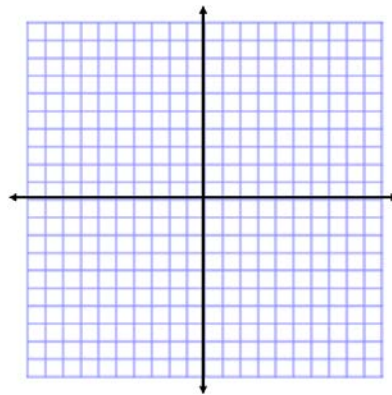
##### i. Graphical Solution

1.  $>$  and  $<$  produce a dotted line, test a point above and below the line to determine a TRUE value
2.  $\geq$  and  $\leq$  produce a solid line, test a point above and below the line to determine a TRUE value

##### ii. Examples

1.  $y \geq -4x + 7$

2.  $y < x - 5$

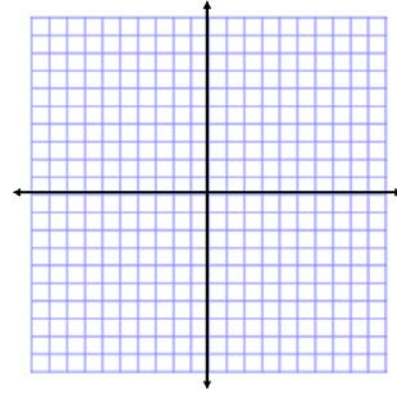


2. Polynomials:

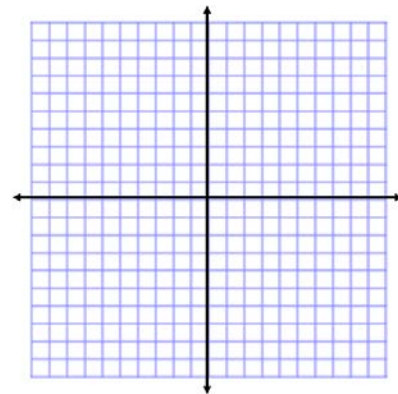
a. Graphical Solution

- i. Calculate the zeroes
- ii. Perform sign analysis to determine the TRUE values
  1. If it is  $\leq$ , the negative values are TRUE
  2. If it is  $\geq$ , the positive values are TRUE
- iii. Examples:

1.  $y > x^4 - 8x^2 + 16$



2.  $y \leq -(x + 4)(x^2 + 5x + 6)$



**Directions:** Solve the following

1.  $4x + 8 \leq 16$

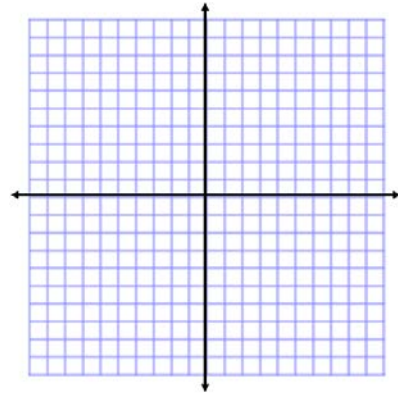
2.  $4x + 7 > 2x - 5$

3.  $-x + 4 \geq 20$

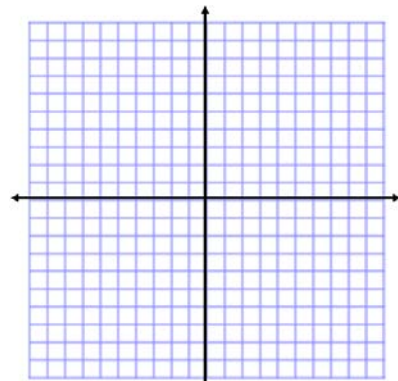
4.  $-2x + 3 < 5 - 3x$

**Directions:** Graph the solutions to the following

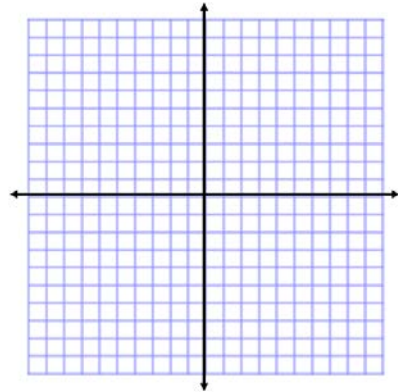
1.  $y \geq -2x + 5$



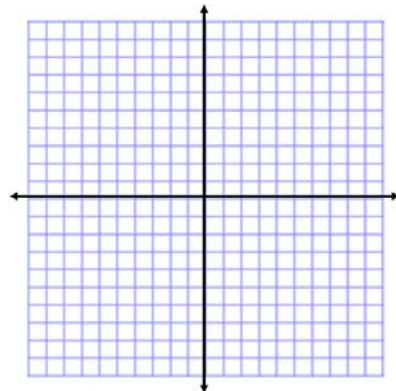
2.  $y < 3x - 4$



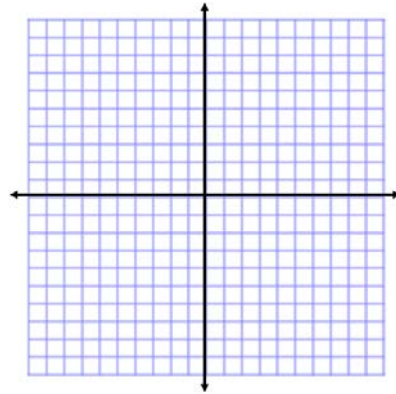
3.  $y \leq -x - 3$



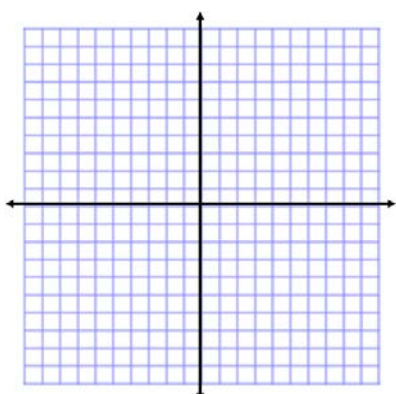
4.  $y > x + 2$



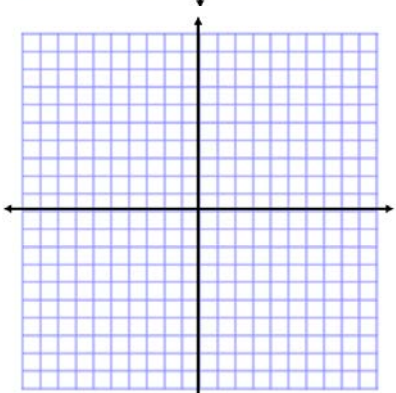
5.  $y \geq -x^2 + 6x - 5$



6.  $y < x(x - 3)(x - 4)$



7.  $y \leq -(x^2 - 4)(x^2 - 16)$



8.  $y > x(x^2 + x - 2)(x^2 + x - 6)$

